

# Algebra I Midterm Review

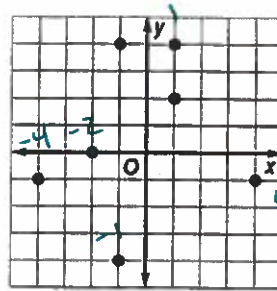
1. What is the domain of the relation shown on the graph?

F  $\{-4, -1, 0, 2, 4\}$

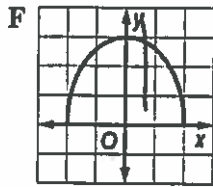
H  $\{-4, -2, -1, 0, 1, 2, 4\}$

G  $\{-4, -2, -1, 1, 4\}$

J  $\{-1, 1\}$



2. Determine which relation is *not* a function.

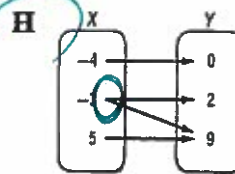


vert  
line  
test

G

x	y
-2	0
0	0
1	2
3	1

no repeats



J

x	y
-4	0
-3	9
5	2
6	9

no repeats

For Questions 3 and 4, use the graph.

3. Interpret the y-intercept of the graph.

A 0 bracelets cost about \$30.

B 1 dozen bracelets cost about \$30.

C 28 dozen bracelets cost \$0.

D Each dozen bracelets costs about \$5.

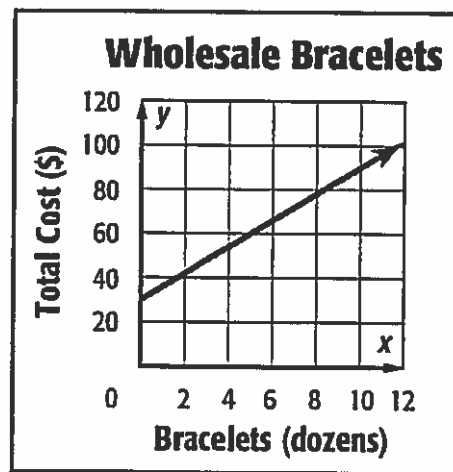
4. Interpret the end behavior of the function.

F The total cost decreases.

G The cost per dozen decreases.

H The total cost increases. (y-value)

J The cost per dozen increases.



5. Solve  $-\frac{3}{8}y = -24$  (reciprocal = -1)

$y = 64$

6. Solve  $5x + 3 = 23$ .

$-3 -3$

$5x = 20$

$x = 4$

7. Solve  $2x + 7 = 5x + 16$ .

$-2x -2x$

$7 = 3x + 16$

$-16 -16$

$-9 = 3x$

$x = -3$

8. Solve  $\frac{2}{3}(6x + 30) = -x + 5(x + 4)$ .

$4x + 20 = 4x + 20$

same

A 6

B 0

C all numbers D no solution

9. Solve  $2x - y = y$  for  $x$ .

A  $x = 2y - 2$

B  $x = y - 2$

C  $x = y$

D  $x = 0$

$2x = 2y$   
 $x = y$

10. In 2005, there were 12,000 students at Beacon High. In 2010, there were 12,250. What is the rate of change in the number of students?

$m = \frac{\Delta y}{\Delta x} = \frac{12000 - 12250}{2005 - 2010} = \frac{-250}{-5} = 50$

11. Elliot's Electricians advertises his rate using the following table. From the information given, determine Elliot's hourly rate.

Hours	2	3	4	5
Charge	\$40	\$60	\$80	\$100

$m = \frac{\Delta y}{\Delta x}$  (any 2 coordinates)

$\frac{60 - 40}{3 - 2} = \frac{20}{1} = 20$

A \$5 per hour

B \$15 per hour

C \$20 per hour

D \$40 per hour

12. What is the slope-intercept form of the equation of a line with a slope of 5 and a y-intercept of -8?

A  $y = -8x + 5$

B  $y = 8x - 5$

C  $5x - y = -8$

D  $y = 5x - 8$

$y = mx + b$

13. Which equation below is parallel to the line graphed at the right?

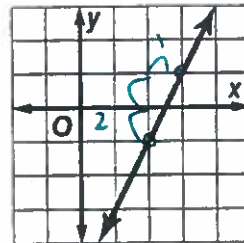
F  $y = -2x + 1$

G  $y = -\frac{1}{2}x + 1$

H  $y = 2x + 1$

J  $y = \frac{1}{2}x + 1$

same slope



$m = \frac{2}{1} = 2$

14. Which is an equation of the line that passes through (2, -5) and (6, 3)?

A  $y = \frac{1}{2}x - 6$

B  $y = \frac{1}{2}x$

C  $y = 2x + 12$

D  $y = 2x - 9$

$m = \frac{-5 - 3}{2 - 6} = \frac{-8}{-4} = 2$

$y - 3 = 2(x - 6)$

$y - 3 = 2x - 12$   
 $+3$   $+3$

15. What is the equation of a horizontal line through (-2, -3)?

F  $x = -2$

G  $y = -3$

H  $-2x - 3y = 0$

J  $-3x + 2y = 0$

16. Find the slope-intercept form of the equation of the line that passes through (-5, 3) and is parallel to  $-3y = -12x + 10$ .

pt. slope  $\rightarrow y - 3 = 4(x + 5)$

Slope int  $\rightarrow y = 4x + 23$

$-3y = -12x + 10$   
 $-3$   $-3$   $-3$   
same  $y = 4x - \frac{10}{3}$

17. If line  $q$  has a slope of  $-\frac{3}{8}$ , what is the slope of any line perpendicular to  $q$ ?

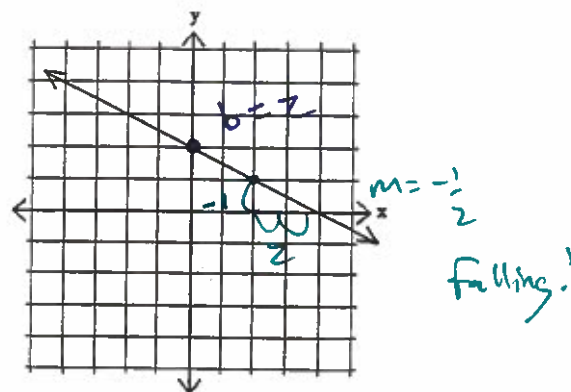
$\perp$  is opp recip

$\frac{8}{3}$

Use the graph to the right for questions 18 and 19.

18. What is the equation, in slope-intercept form, of the line graphed?

$$y = -\frac{1}{2}x + 2$$



19. Fill out the table:

Domain:	$\mathbb{R}$
Range:	$\mathbb{R}$
x-intercept:	(4, 0)
y-intercept:	(0, 2)
End Behavior:	As $x$ increases, $y$ approaches $-\infty$ As $x$ decreases, $y$ approaches $\infty$

20. Find the slope-intercept form of the equation that passes through (2, 3) and is perpendicular to  $y = -\frac{1}{3}x - 5$

$$y - 3 = 3(x - 2)$$

$$y = 3x - 3$$

$$m = -\frac{1}{3}$$

$$\perp m = 3$$

21. Find the inverse of  $\{(4, -1), (3, -2), (6, 9), (8, 5)\}$ .

F  $\{(8, 5), (6, 9), (3, -2), (4, -1)\}$

H  $\{(-1, 4), (-2, 3), (9, 6), (5, 8)\}$

G  $\{(-4, 1), (-3, 2), (-6, -9), (-8, -5)\}$

J  $\{(-1, -2), (9, 5), (4, 3), (6, 8)\}$

22. If  $f(x) = 3x - 4$ , find  $f^{-1}(x)$ .

A  $f^{-1}(x) = 4x - 3$

C  $f^{-1}(x) = \frac{x-4}{3}$

B  $f^{-1}(x) = \frac{x+4}{3}$

D  $f^{-1}(x) = -4 - 3x$

$$y = 3x - 4$$

$$x = 3y - 4 \text{ (now solve for 'y')}$$

$$x + 4 = 3y$$

$$\frac{x}{3} + \frac{4}{3} = y$$

23. The table of values represents all points in the function  $f(x)$ . What is the value of  $f^{-1}(2)$ ?

A. 0

B. 1

C. 4

D. 6

$x$	$f(x)$
0	2
1	4
2	6

$x$	$f^{-1}(x)$
2	0
4	1
6	2

24. Solve:  $-51 \leq x + 38$

$$-38 \quad -38$$

$$-89 \leq x$$

also written

$$x \geq -89$$

26. Solve:  $4w - 6 > 6w - 20$

$$-4w \quad -4w$$

$$-6 > 2w - 20$$

$$+20 \quad +20$$

$$14 > 2w$$

$$7 > w$$

also written

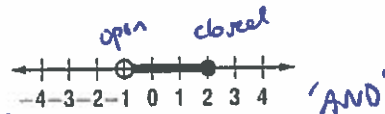
$$w < 7$$

25. Solve:  $\frac{t}{-2} > 4(-2)$

$$t < -8$$

↑ switch sign

27. Which compound inequality has the solution set shown in the graph?



~~A~~  $-1 < n < 2$

~~B~~  $-1 ≤ n < 2$

~~C~~  $n ≥ -1$  or  $n < 2$

D  $-1 < n ≤ 2$

28. Which of the following is the solution set of  $-4 < 3t + 5 ≤ 20$ ?

F  $-3 < t ≤ 5$

G  $-3 < t ≤ 5$

whoops

H  $t < -3$  or  $t > 5$

J  $t < -3$  or  $t ≥ 5$

$$\frac{-9}{3} < \frac{3t}{3} ≤ \frac{15}{3}$$

$-3 < t ≤ 5$

29. Which of the following is the solution set of  $|2x - 3| > 4$ ?

A  $x < -0.5$  or  $x > 3.5$

B  $x < -1$  or  $x > 7$

C  $-0.5 < x < 3.5$

D  $x < 0.5$  or  $x > 3.5$

$$2x - 3 > 4 \quad \text{OR} \quad 2x - 3 < -4$$
  

$$+3 \quad +3 \quad \quad \quad +3 \quad +3$$

$$\frac{x}{2} > \frac{7}{2} \quad \text{OR} \quad \frac{x}{2} < -\frac{1}{2}$$

$x > \frac{7}{2}$  OR  $x < -\frac{1}{2}$

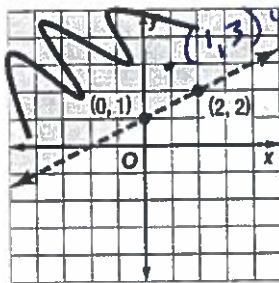
30. Which inequality is graphed at the right?

~~E~~  $y < 2x + 1$

~~G~~  $y > 2x + 1$

H  $y < \frac{1}{2}x + 1$

J  $y > \frac{1}{2}x + 1$



$3 < \frac{1}{2}(1) + 1$

~~$3 < 1.5$~~

$3 > \frac{1}{2}(1) + 1$

$3 > 1.5$

31. Determine which of the ordered pairs are a part of the solution of  $y + 1 > \frac{1}{2}x + 3$ .

F (2, 3)

G (-4, 0)

H (1, 2)

J (-3, 1)

~~$4 > 4$~~

~~$1 > 1$~~

~~$3 > 3.5$~~

$2 > 1.5$

Plug in to see what works!

32. Laurie and Maya sold at most \$50 worth of get-well and friendship cards. The friendship cards,  $x$ , were sold for \$2 each and the get-well cards,  $y$ , were sold for \$1.50 each. Which point represents a reasonable number of cards sold?

F (20, 10)

G (15, 10)

H (18, 20)

J (10, 30)

~~$55 ≤ 50$~~

$45 ≤ 50$

~~$66 ≤ 50$~~

~~$65 ≤ 50$~~

$2x + 1.50y ≤ 50$

33. Which statement is true about the solution to the system of equations?

$$\begin{aligned} y + 4 &= -\frac{1}{2}x - 4 \\ x + 2y &= -8 \end{aligned}$$

$y = -\frac{1}{2}x - 4$

- A. The two lines intersect at exactly one point.
- B. The two lines do not intersect.
- C. The two lines intersect at exactly 2 points.
- D. The two lines coincide.

$$x + 2\left(-\frac{1}{2}x - 4\right) = -8$$

$$x + x - 8 = -8$$

$-8 = -8$

interpret

many

50....

34. Solve the system if  $x = 2y + 3$  and  $4x - 5y = 9$ .

$$4(2y + 3) - 5y = 9$$

$$8y + 12 - 5y = 9$$

$$3y = -3$$

$y = -1$

plug into original

$x = 1$

$(1, -1)$

✓ it

35. Solve the system if  $(x - 5y = 20)$  and  $x + 3y = -4$ .

$$8y = -24$$

$$y = -3$$

$$x - 5(-3) = 20$$

$$x + 15 = 20$$

$$x = 5$$

$$(5, -3)$$

36. Your teacher is giving a test that has 4-point questions (x) and 6-point questions (y). The test has 25 total questions and is worth 120 points. Which system represents this information?

A  $x + y = 120$   
 $4x + 6y = 25$

B  $x + y = 25$   
 $4x + 4y = 120$

C  $x - y = 25$   
 $6x + 4y = 120$

D  $x + y = 25$  ← ?  
 $4x + 6y = 120$  ← Pts

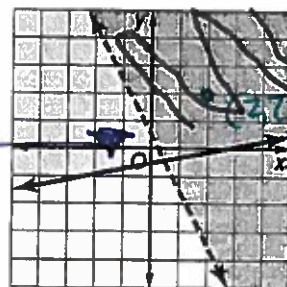
37. What system of inequalities is represented in the graph?

F  $y < -2x + \frac{1}{2}$   
 $y \leq \frac{1}{5}x - \frac{1}{2}$

G  $y > -2x + \frac{1}{2}$   
 $y \leq \frac{1}{5}x - \frac{1}{2}$

H  $y < -2x + \frac{1}{2}$   
 $y \geq \frac{1}{5}x - \frac{1}{2}$

J  $y > -2x + \frac{1}{2}$   
 $y \geq \frac{1}{5}x - \frac{1}{2}$



← overlap

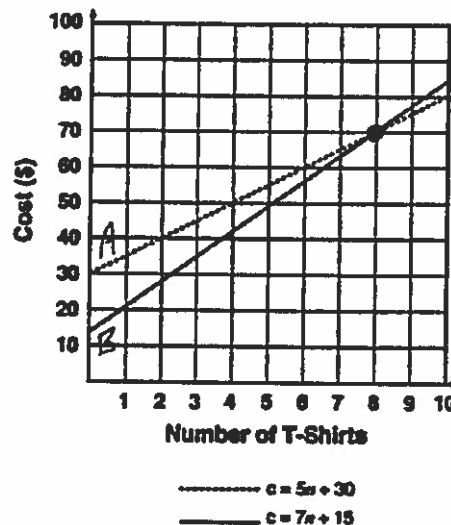
Solid line shade up result so  $\geq$

Dashed + up so  $>$

(2, 2) should work

38. A club will create t-shirts for a fundraiser. The club members need to compare the cost of creating the t-shirts between two companies. Company A charges \$30 for setup, plus \$5 per t-shirt. Company B charges \$15 for setup, plus \$7 per t-shirt. The situation is shown on the graph to the right.

How many t-shirts are manufactured for the cost to be equal?



39. Simplify  $(x^3)^8$ .

$$x^{24}$$

40. Simplify  $(-2hk)^4(4h^3k^5)^2$ .

$$(-2)^4 h^4 k^4 (4)^2 h^6 k^{10} = 4^2 (-2)^4 h^{10} k^{14}$$

41. Simplify  $\frac{3ab^4c^2b^1}{9b^1c^5}$ . Assume the denominator is not equal to zero.

$$\frac{4b^5}{1c^3}$$

42. Simplify  $\frac{(3y^4n^6)^2}{(y^2n^{-3})^4}$ . Assume the denominator is not equal to zero.

F  $\frac{9}{y^{16}}$

G  $\frac{9}{n^{24}}$

H  $9y^{16}$

J  $9n^{24}$

$$\frac{3^2 y^8 n^{12}}{y^8 n^{-12}} = 3^2 y^0 n^{24} = 9n^{24}$$



43. Write  $10y^{\frac{1}{2}}$  in radical form.

A  $\sqrt{10y}$

B  $10\sqrt{y}$

C  $10\sqrt{10y}$

D  $y\sqrt{10}$

44. Evaluate  $81^{\frac{3}{4}}$ .

$\sqrt[4]{81^3}$

or 27

45. Which equation represents exponential growth?

A  $y = 5(0.84)^x$

B  $y = 5x$

C  $y = 0.3x^3$

D  $y = 5(1.06)^x$

↑  
decay

linear

cubic

↑  
> 1

Use the graph shown to the right to answer questions 46 – 47.

46. Which equation corresponds to the graph shown?

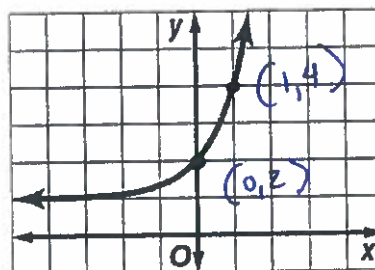
F  $y = (3)^{x+1}$

G  $y = 2(3^x + 1)$

(1, 4) doesn't work

H  $y = 2(3^x)$

J  $y = (2 \cdot 3)^{x+1}$



47. Find the domain and range

D:  $\mathbb{R}$

R:  $y > 1$

48. Solve:  $2^{5x+4} = 512$

$2^{5x+4} = 2^9$

$5x+4 = 9$

$-4 -4$

$5x = 5$

$x = 1$

✓ 12!

$2^{5(1)+4} = 512$

$512 = 512$

49. A certain fast-growing bacteria increases 6% per minute. If there are 100 bacteria now, about how many will there be 12 minutes later?

F 172

G 201

H 48

J 190

.06

$100(1.06)^{12}$

201.2196...

50. A city's population is about 954,000 and is decreasing at an annual rate of 0.1%. Predict the population in 50 years.

A 577,176

B 906,300

C 1,002,888

D 907,450

.001

$954,000(1-.001)^{50}$

907,450.1693