

For 1- 3, find each value.

1. If $\csc A = 2$, find the value of $\sin A$.

2. If $\cos \theta = \frac{1}{4}$ and $0^\circ < \theta < 90^\circ$, find $\tan \theta$.

3. If $\cot x = -\frac{3}{2}$ and $\sec x < 0$, find $\sin x$ and $\cos x$.

For 4 - 8, simplify each expression.

4. $\sin x \sec x$

5. $\cot x \sec x \sin x$

6. $\cos x + \sin x \tan x$

7. $\frac{\cot A}{\tan A}$

8. $\sin^2 \theta \cos^2 \theta - \cos^2 \theta$

9. $\frac{\sin x \csc x}{\tan x}$

10. $\tan x \cot x - \cos^2 x$

11. $\frac{\sin x}{\cos x} + \frac{\cos x}{1 + \sin x}$

For 12 - 16, verify each identity.

$$12. \quad \frac{\sin \theta}{1 + \cos \theta} + \frac{1 + \cos \theta}{\sin \theta} = 2 \csc \theta$$

$$13. \quad \frac{\csc \theta \tan \theta}{1 + \tan^2 \theta} = \cos \theta.$$

$$14. \quad \frac{1}{\sec x - \tan x} = \sec x + \tan x$$

$$15. \quad 2 \tan x \sec x = \frac{1}{1 - \sin x} - \frac{1}{1 + \sin x}$$

$$16. \quad \frac{\cos x}{1 - \sin x} = \sec x + \tan x$$