

Name: key

5.4 & 5.5(part 1) Practice Problems

1) Find the exact value: $\cos 195^\circ$

$$\cos(135^\circ + 60^\circ)$$

$$\cos 135^\circ \cos 60^\circ - \sin 135^\circ \sin 60^\circ$$

$$\left(-\frac{\sqrt{2}}{2}\right)\left(\frac{1}{2}\right) - \left(\frac{\sqrt{2}}{2}\right)\left(\frac{\sqrt{3}}{2}\right)$$

$$\frac{-\sqrt{2} - \sqrt{6}}{4}$$

2) Find the exact value: $\sin \frac{13\pi}{12}$ or 195°

$$\sin\left(\frac{10\pi}{12} + \frac{3\pi}{12}\right)$$

$$\sin\left(\frac{5\pi}{6} + \frac{\pi}{4}\right)$$

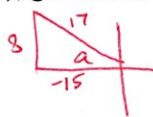
$$\sin \frac{5\pi}{6} \cos \frac{\pi}{4} + \cos \frac{5\pi}{6} \sin \frac{\pi}{4}$$

$$\frac{1}{2} \left(\frac{\sqrt{2}}{2}\right) + \left(\frac{\sqrt{3}}{2}\right)\left(\frac{\sqrt{2}}{2}\right)$$

$$\frac{+\sqrt{2} - \sqrt{6}}{4}$$

$$\frac{\sqrt{2} - \sqrt{6}}{4}$$

3) Find $\cos(a - b)$, given that $\sin a = \frac{8}{17}$ with $\frac{\pi}{2} < a < \pi$ and $\cos b = \frac{1}{2}$ with $0 < b < \frac{\pi}{2}$



Q2

Q1



$$\cos a \cos b + \sin a \sin b$$

$$\left(\frac{-15}{17}\right)\left(\frac{1}{2}\right) + \left(\frac{8}{17}\right)\left(\frac{\sqrt{3}}{2}\right)$$

$$\frac{-15}{34} + \frac{8\sqrt{3}}{34}$$

$$\frac{-15 + 8\sqrt{3}}{34}$$

4) Find the exact value: $\tan(-15^\circ)$ or $\tan 345^\circ$

$$\tan(30^\circ - 45^\circ)$$

$$\frac{\tan 30^\circ - \tan 45^\circ}{1 + \tan 30^\circ \tan 45^\circ}$$

$$\frac{\frac{\sqrt{3}}{3} - 1}{1 + \left(\frac{\sqrt{3}}{3}\right)(1)}$$

$$\frac{\frac{\sqrt{3}-3}{3} (3-\sqrt{3})}{\frac{3+\sqrt{3}}{3} (3-\sqrt{3})}$$

$$\frac{-6 + 6\sqrt{3}}{9 - \sqrt{9}}$$

$$\frac{-6 + 6\sqrt{3}}{6}$$

$$-1 + \sqrt{3}$$

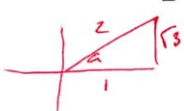
5) Find the exact value: $\sin(75^\circ)$ $\sin(30^\circ + 45^\circ)$

$$\sin 30^\circ \cos 45^\circ + \cos 30^\circ \sin 45^\circ$$

$$\left(\frac{1}{2}\right)\left(\frac{\sqrt{2}}{2}\right) + \left(\frac{\sqrt{3}}{2}\right)\left(\frac{\sqrt{2}}{2}\right)$$

$$\frac{\sqrt{2} + \sqrt{6}}{4}$$

6) Given $\cos a = \frac{1}{2}$ with $0 < a < \frac{\pi}{2}$, find $\sin 2a$ and $\tan \frac{a}{2}$.



Q1

$$2 \sin a \cos a$$

$$2 \left(\frac{\sqrt{3}}{2}\right)\left(\frac{1}{2}\right)$$

$$\frac{\sqrt{3}}{2}$$

$$\frac{1 - \frac{1}{2}}{\frac{\sqrt{3}}{2}}$$

$$\frac{\frac{1}{2}}{\frac{\sqrt{3}}{2}}$$

$$\frac{1}{\sqrt{3}}$$

$$\frac{\sqrt{3}}{3}$$

7) Find the exact value: $\cos \frac{2\pi}{3} \cos \frac{\pi}{4} + \sin \frac{2\pi}{3} \sin \frac{\pi}{4}$

$$\cos\left(\frac{\pi}{2} - \frac{\pi}{4}\right)$$

$$\cos\left(\frac{2\pi}{4} - \frac{\pi}{4}\right)$$

$$\cos \frac{\pi}{4}$$

$$\frac{\sqrt{2}}{2}$$

8) Simplify: $\tan(x - 2\pi)$

$$\frac{\tan x - \tan 2\pi}{1 + \tan x \tan 2\pi}$$

$$\frac{\tan x - 0}{1 + \tan x(0)}$$

$$\tan x$$