

For numbers 1 and 2, use the given information to find the exact value of each of the following.

a) $\sin 2\theta$

1. $\sin \theta = \frac{15}{17}$, $\theta, \frac{\pi}{2} < \theta < \pi$
Q2 

$$\begin{aligned}\sin 2\theta &= 2 \sin \theta \cos \theta \\ &= 2 \left(\frac{15}{17} \right) \left(-\frac{8}{17} \right) \\ &= -\frac{240}{289}\end{aligned}$$

b) $\cos 2\theta$

$$\begin{aligned}1 - 2 \sin^2 \theta \\ 1 - 2 \left(\frac{15}{17} \right)^2\end{aligned}$$

$$\frac{-514}{289}$$

c) $\tan 2\theta$

$$\begin{aligned}\frac{2 \tan \theta}{1 - \tan^2 \theta} \\ \frac{2 \left(\frac{15}{-8} \right)}{1 - \left(\frac{15}{-8} \right)^2} \\ \frac{\frac{15}{-4}}{-\frac{161}{64}}\end{aligned}$$

2. $\cot \theta = 2$, $\cos \theta < 0$

$\tan = \frac{1}{2}$

$\tan \rightarrow +\frac{1}{2}$
 $\cos \rightarrow -\frac{2}{\sqrt{5}}$

a) $\sin 2\theta = 2 \sin \theta \cos \theta$
 $= 2 \left(\frac{1}{\sqrt{5}} \right) \left(-\frac{2}{\sqrt{5}} \right)$
 $= -\frac{4}{5}$

b) $1 - 2 \sin^2 \theta$
 $1 - 2 \left(\frac{1}{\sqrt{5}} \right)^2$
 $1 - \frac{2}{5}$
 $\frac{3}{5}$

c) $2 \left(\frac{1}{2} \right)$
 $1 - \left(\frac{1}{2} \right)^2$
 $\frac{1}{1 - \frac{1}{4}}$

$\frac{960}{644}$ or $\frac{240}{161}$
 $\frac{1}{\frac{3}{4}}$
 $\frac{4}{3}$

For numbers 3 and 4, write each expression as the sine, cosine, or tangent of a double angle. Then find the exact value of the expression.

3. $2 \sin 15^\circ \cos 15^\circ$

$\sin 2\theta$
 $\sin 2(15^\circ)$
 $\sin 30^\circ$
 $\frac{1}{2}$

4. $2 \cos^2 \frac{\pi}{8} - 1$

$\cos 2\theta$
 $\cos 2 \left(\frac{\pi}{8} \right)$
 $\cos \frac{\pi}{4}$
 $\frac{\sqrt{2}}{2}$

For numbers 5 - 7, use a half-angle formula to find the exact value of each expression.

5. $\cos 22.5^\circ$

$\cos \frac{45^\circ}{2} = \pm \sqrt{\frac{1 + \cos 45^\circ}{2}}$
 $= \pm \sqrt{\frac{1 + \frac{\sqrt{2}}{2}}{2}}$
 $= \pm \sqrt{\frac{2 + \sqrt{2}}{2}}$
 $\frac{\sqrt{2 + \sqrt{2}}}{2}$

6. $\tan 112.5^\circ$

$\tan \frac{225^\circ}{2}$
 $\frac{1 - \cos 225^\circ}{\sin 225^\circ}$
 $\frac{1 - (-\frac{\sqrt{2}}{2})}{(-\frac{\sqrt{2}}{2})}$
 $\frac{2 + \sqrt{2}}{-\sqrt{2}}$
 $\frac{-2 - \sqrt{2}(\sqrt{2})}{\sqrt{2}(\sqrt{2})}$
 $\frac{-2\sqrt{2} - 2}{2}$
 $-\sqrt{2} - 1$

7. $\tan \frac{7\pi}{8}$

$\tan \frac{7\pi}{4}$
 $\frac{2 - \sqrt{2}(-\sqrt{2})}{-\frac{\sqrt{2}}{2}(-\sqrt{2})}$
 $\frac{-2\sqrt{2} + 2}{2}$
 $\frac{1 - \cos \frac{7\pi}{4}}{\sin \frac{7\pi}{4}}$
 $\frac{1 - \frac{\sqrt{2}}{2}}{-\frac{\sqrt{2}}{2}}$
 $\frac{-\sqrt{2} + 1}{1}$
 $-\sqrt{2} + 1$