

Unit 7 Review

Simplify each expression

$$1) \sqrt{50} + \sqrt{32} = \sqrt{2} - \frac{1}{\sqrt{2}} = \frac{9\sqrt{2}}{2} - \frac{\sqrt{2}}{2} = \frac{18\sqrt{2} - \sqrt{2}}{2} = \frac{17\sqrt{2}}{2}$$

$$\boxed{5\sqrt{2} + 4\sqrt{2}} \quad \frac{1}{\sqrt{2}}$$

a) $4\sqrt{2}$ If
You can
reduce
this
you're
in good
shape!

$$b) \sqrt{2} - \frac{\sqrt{2}}{2}$$

$$c) \frac{17\sqrt{2}}{2}$$

$$d) 17\sqrt{2}$$

$$2) \sqrt{6}(\sqrt{10} + \sqrt{15}) = \sqrt{60} + \sqrt{90} = 2\sqrt{15} + 3\sqrt{10}$$

$$a) 5\sqrt{25}$$

$$b) 5\sqrt{10}$$

$$c) 3\sqrt{15} + 2\sqrt{10}$$

$$d) 2\sqrt{15} + 3\sqrt{10}$$

$$3) (\sqrt{2} + 2\sqrt{8})(3\sqrt{6} - \sqrt{5}) = 3\sqrt{12} - \sqrt{10} + 6\sqrt{48} - 2\sqrt{40} = 3(2\sqrt{3}) - \sqrt{10} + 6(4\sqrt{3}) - 2(2\sqrt{10})$$

$$a) 18\sqrt{3} - 5\sqrt{10}$$

$$b) 6\sqrt{3} - 4\sqrt{10}$$

$$c) 30\sqrt{3} - 5\sqrt{10}$$

$$d) 25\sqrt{3} - \sqrt{10}$$

$$\underline{6\sqrt{3} - \sqrt{10} + 24\sqrt{3} - 4\sqrt{10}}$$

$$\underline{-}$$

$$4) (5 - \sqrt{15})^2 = 25 - 10\sqrt{15} + 15$$

$$a) 10$$

$$b) 15 - 10\sqrt{15}$$

$$c) 40 - 10\sqrt{15}$$

$$d) 10 - 10\sqrt{15}$$

$$5) 5\sqrt{19} + 4\sqrt{28} - 8\sqrt{19} + \sqrt{63}$$

$$a) 3\sqrt{19} + 11\sqrt{7}$$

$$b) \cancel{-3}\sqrt{19} + 11\sqrt{7}$$

$$c) 8\sqrt{26}$$

$$d) 13\sqrt{19} + 11\sqrt{7}$$

$$6) (\sqrt{m-5})^2 = (4\sqrt{3})^2$$

a) 43

b) 53

c) 73

d) 17

$$\begin{array}{r} m-9=16(3) \\ \cancel{+9} \quad +9 \\ m=53 \end{array}$$

$$4\sqrt{3} = 4\sqrt{3}$$

$$7) y^2 = (\sqrt{y+6})^2$$

a) -2

b) \emptyset

c) 0

d) 3

$$\begin{aligned} y^2 &= y+6 \\ y^2 - y - 6 &= 0 \end{aligned} \quad \rightarrow (y-3)(y+2) = 0$$

$$\boxed{-3}$$

Extraneous

$$8) \sqrt{10p+61} - 7 = p$$

$$\rightarrow \quad \rightarrow$$

$$c) -\frac{59}{7}$$

a) -6

b) \emptyset

d) -6, 2

$$10p+61 = (p+7)^2$$

$$0 = p^2 + 14p + 49 - 10p - 61$$

$$0 = p^2 + 4p - 12$$

$$0 = (p+6)(p-2)$$

$$\boxed{-6, 2}$$

$$9) \sqrt{2x+15} + 5 = 18$$

a) 77

b) -16

c) -1

d) 28

$$\begin{array}{l} 2x+15 = 169 \\ \cancel{+15} \quad \cancel{-15} \\ 2x = 154 \\ \cancel{\times 2} \end{array}$$

$$18 \checkmark$$

77

$$10) \frac{2h}{h-1} \times \frac{2h+1}{h+2}$$

-2, 1 could be extraneous; excluded

$$a) -\frac{1}{5}$$

b) -5

$$c) -\frac{1}{5}; \text{extraneous: } -2, 1$$

$$d) \frac{1}{5}$$

$$zh(h+2) = (h-1)(2h+1)$$

$$zh^2 + 2h = 2h^2 - h - 1$$

$$\frac{5h}{5} = -1$$

$$h = -\frac{1}{5}$$

$$18) \quad 11) \quad \left[\frac{2q-1}{6} - \frac{q}{3} = \frac{q+4}{18} \right]$$

a) -7

b) no solution

c) 7

d) $\frac{7}{17}$

$$3(2q-1) - 6q = q + 4$$

✓ it's

$$6q - 3 - 6q = q + 4$$

$$\frac{-15}{6} + \frac{7}{3} = \frac{-3}{18}$$

$-7 = q$

$$\frac{-45}{18} + \frac{42}{18} = \frac{-3}{18}$$

$$12) \quad \frac{5}{p-1} - \frac{3}{p+2} = 0 \quad \text{exclude } -2, 1$$

a) $-\frac{13}{2}$; extraneous: -2 b) $\frac{13}{2}$

$$\frac{-3}{18} \checkmark \frac{-3}{18}$$

c) $\frac{7}{2}$

d) $-\frac{13}{2}$

$$\frac{5}{p-1} \cancel{\times} \frac{3}{p+2}$$

$$5p + 10 = 3p - 3$$

$$2p = -13$$

$p = -\frac{13}{2}$

✓

$$p = 0$$

$$13) \quad \left[\frac{n+2}{n} + \frac{n+5}{n+3} = -\frac{1}{n} \right] \quad \text{exclude } -3, 0$$

a) $-\frac{9}{2}$; extraneous: -1

b) -1; extraneous: -3

c) $-\frac{9}{2}, -1$

d) -9, -2

$$(n+3)(n+2) + n(n+5) = -1(n+3)$$

$$n^2 + 5n + 6 + n^2 + 5n = -n - 3$$

$$2n^2 + 10n + 9 = 0$$

$$(2n+9)(n+1) = 0$$

$$-4 + \frac{4}{2} = 0$$

$\cancel{0} \neq 1$

OKAY!

✓ (-9/2)

$$\frac{-2.5}{-4.5} + \frac{.5}{-1.5} = \frac{-1}{-4.5}$$

$$\frac{5}{7} + \frac{-1}{3} = \frac{2}{9}$$

$$\frac{5}{9} + \frac{3}{9} = \frac{2}{9}$$

$$\frac{2}{7} \checkmark \frac{2}{7}$$

$\cancel{x} + \cancel{-\frac{9}{2}}$
extraneous!!!

$$(p-2)(p+2)$$

exclude ± 2

14) $\left[\frac{2p}{p-2} + \frac{p+2}{p^2-4} = 1 \right]$

- a) $-\frac{1}{3}$ b) $-\frac{1}{3}$; extraneous: -2 c) -3, -2 d) -3; extraneous: -2

$$2p(p+2) + p+2 = (p-2)(p+2)$$

$$2p^2 + 4p + p + 2 = p^2 - 4$$

$$p^2 + 5p + 6 = 0$$

$$(p+3)(p+2) = 0$$

$$\boxed{-3, -2}$$

extraneous

$$\frac{\sqrt{-3}}{5}$$

$$\frac{-6}{-5} + \frac{-1}{5} = 1$$

$$1 = 1$$

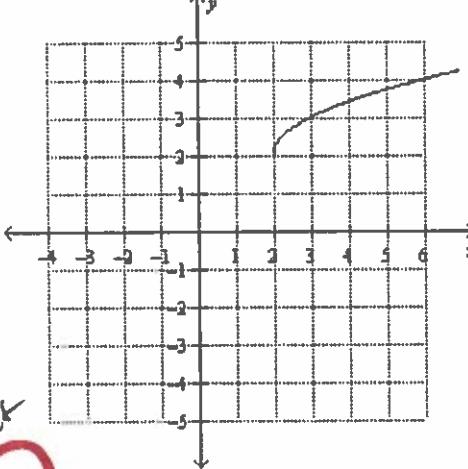
$$\frac{\sqrt{-2}}{5}$$

$$\frac{-4}{-4} + \frac{-2}{0} = 1$$

15) Which state below describes and shows the graph of $y = -\sqrt{x-2} + 2$

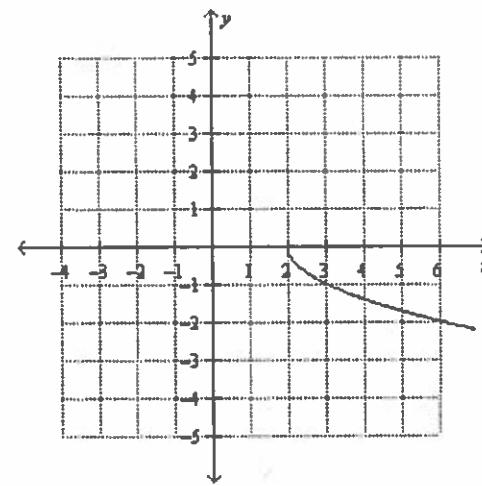


translation of $y = \sqrt{x}$ up 2 units and right 2 units;
 $D = \{x | x \geq 2\}$,
 $R = \{y | y \leq 2\}$

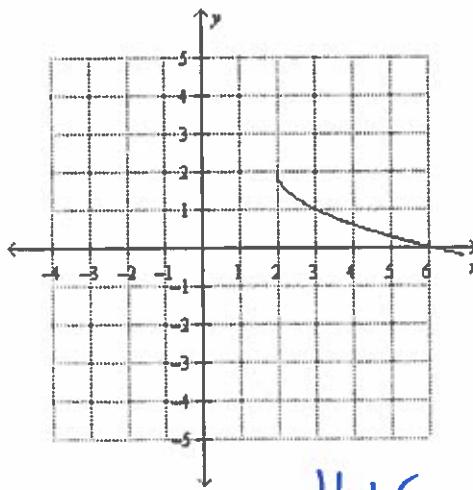


correct

b) translation of $y = \sqrt{x}$ right 2 units, reflected in the x-axis;
 $D = \{x | x \geq 2\}$,
 $R = \{y | y \leq 2\}$

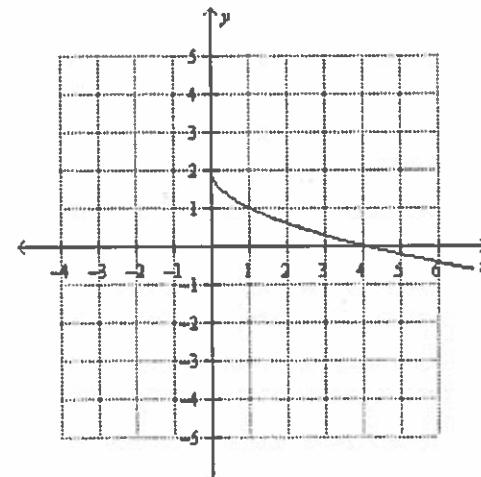


c) translation of $y = \sqrt{x}$ up 2 units and right 2 units,
reflected in the x-axis;
 $D = \{x | x \geq 2\}$,
 $R = \{y | y \leq 2\}$



#16 \rightarrow A

d) translation of $y = \sqrt{x}$ up 2 units reflected in the x-axis;
 $D = \{x | x \geq 2\}$,
 $R = \{y | y \leq 2\}$



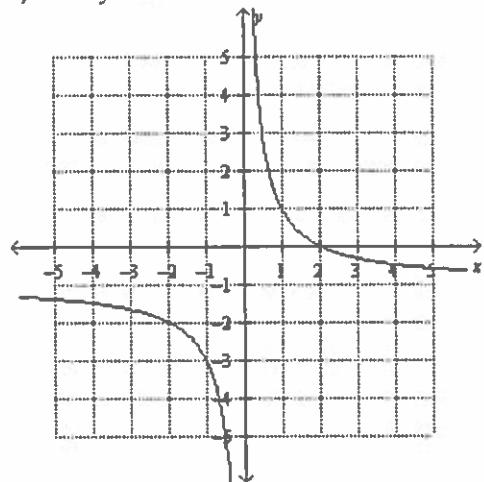
17) Graph $y = \frac{2}{x-1}$ and identify the asymptotes.

center $(1, 0)$

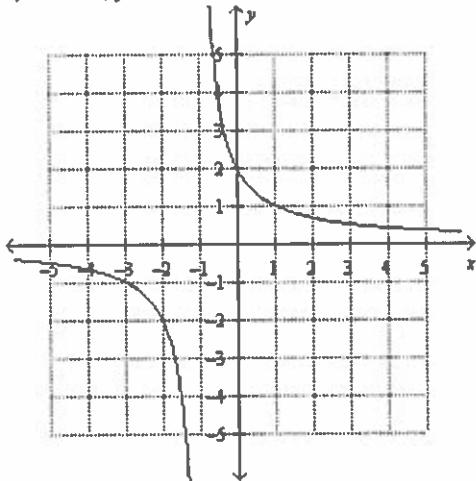
$$x=1$$

$$y=0$$

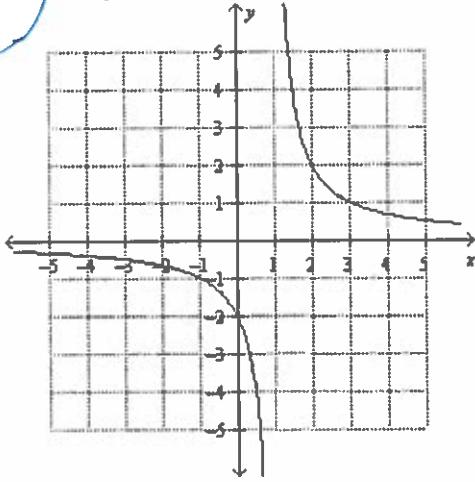
b) $x=0, y=-1$



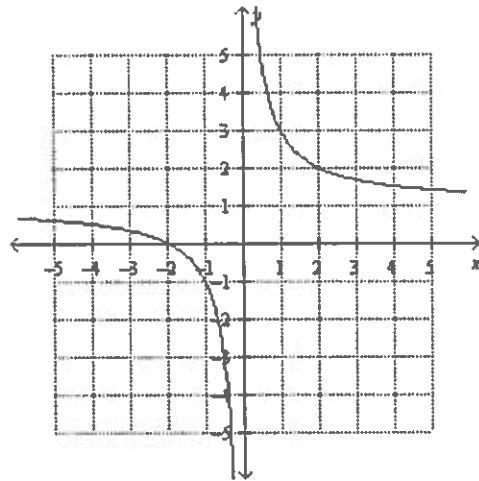
a) $x=-1, y=0$



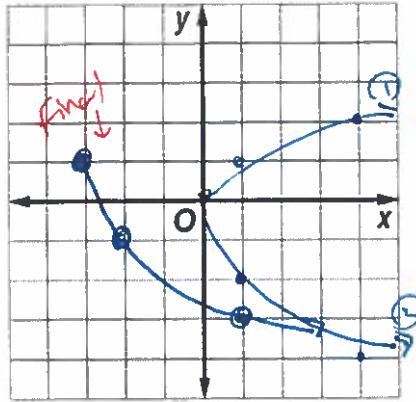
c) $x=1, y=0$



d) $x=0, y=1$



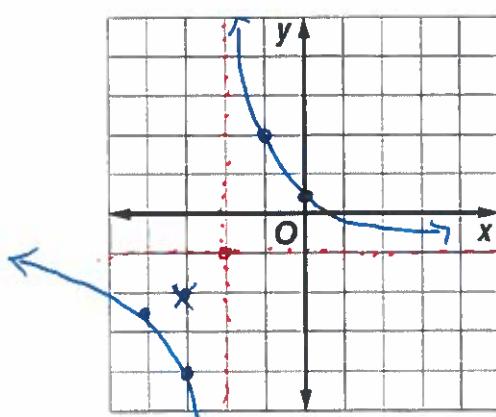
18) Graph $g(x) = -2\sqrt{x+3} + 1$



Domain: $x \geq -3$

Range: $y \leq 1$

19) Graph $g(x) = \frac{3}{x+2} - 1$ *center* $(-2, -1)$



x	y
-1	2
0	0.5
-3	-4
-4	-2.5

Vertical Asymptote: $x = -2$

Horizontal Asymptote: $y = -1$

Domain: $x \neq -2$

Range: $y \neq -1$