

1. Find the exact value of $\cos 15^\circ$.

F $\frac{-\sqrt{2}-\sqrt{6}}{4}$

G $\frac{\sqrt{6}-\sqrt{2}}{4}$

H $\frac{\sqrt{6}+\sqrt{2}}{4}$

J $\frac{\sqrt{2}-\sqrt{6}}{4}$

2. Solve $\sin x - \sin^2 x = 0$ on the interval $[0, 2\pi)$.

A $0, \pi, \frac{\pi}{2}$
B $\frac{\pi}{2}$

C $\frac{\pi}{2}, \frac{3\pi}{2}$
D $\pi, \frac{\pi}{4}$

3. Find the exact value of $\cos \frac{\pi}{8}$.

F $-\frac{\sqrt{2}-\sqrt{2}}{2}$

G $-\frac{\sqrt{2}+\sqrt{2}}{2}$

H $\frac{\sqrt{2}-\sqrt{2}}{2}$

J $\frac{\sqrt{2}+\sqrt{2}}{2}$

4. Simplify $\frac{\sec \theta \tan \theta}{\sin \theta}$.

A $\sec^2 \theta$

B $\cot \theta$

C $\tan^2 \theta$

D $\cos^2 \theta$

5. If $\csc \theta = -\frac{5}{4}$ on the interval $(270^\circ, 360^\circ)$, find $\tan \theta$.

F $-\frac{4}{3}$

G $\frac{3}{4}$

H $\frac{4}{3}$

J $-\frac{4}{5}$

6. Simplify $\frac{\cos x}{\sec x - 1} + \frac{\cos x}{\sec x + 1}$.

F $2 \tan^2 x$

G $2 \cos x$

H $2 \cos^2 x - 1$

J $2 \cot^2 x$

7. If $\csc \theta = -\frac{5}{3}$ on the interval $\left(\pi, \frac{3\pi}{2}\right)$, find the exact value of $\tan 2\theta$.

A $\frac{24}{25}$

B $-\frac{7}{25}$

C $\frac{24}{7}$

D $\frac{7}{25}$

8. Solve $2 \sin x - \sqrt{3} = 0$ on the interval $[0, 2\pi)$.

A $\frac{\pi}{6}, \frac{5\pi}{6}$

B $\frac{\pi}{3}, \frac{2\pi}{3}$

C $\frac{\pi}{3}, \frac{5\pi}{3}$

D $\frac{7\pi}{6}, \frac{11\pi}{6}$

9. Find the exact value of $\cos 67.5^\circ$.

F $-\frac{\sqrt{2-\sqrt{2}}}{2}$

G $-\frac{\sqrt{2+\sqrt{2}}}{2}$

H $\frac{\sqrt{2-\sqrt{2}}}{2}$

J $\frac{\sqrt{2+\sqrt{2}}}{2}$

10. Verify: $\cos \theta \tan^2 \theta + \cos \theta = \sec \theta$

11. Simplify $\csc \theta - \cot \theta \cos \theta$.

12. Find the exact value of $\cos 255^\circ$.

13. Find the exact value of $\frac{\tan 25^\circ + \tan 35^\circ}{1 - \tan 25^\circ \tan 35^\circ}$

14. Solve on the interval $[0, 2\pi)$: $\cos 2\theta + 2\cos^2 \theta = 0$

15. Solve on the interval $[0, 2\pi)$: $\cos \theta \sin 2\theta = 0$

16. Verify: $\frac{1 - \sin^2 \theta}{1 - \cos^2 \theta} = \cot^2 \theta$.

17. If $\cos \theta = \frac{4}{5}$ on the interval $\left(\frac{3\pi}{2}, 2\pi\right)$, find the exact value of $\tan 2\theta$.

18. Solve $\tan x - \sqrt{3} = 0$ on the interval $[0, 2\pi)$.

19. Find the exact value of $\cos \frac{7\pi}{12}$.

For 20-22, Find all solutions on the interval $[0, 2\pi)$.

20. $\sin^2 x - 2 \sin x = 3$

$$21. \sin^2 x - \sin x + 1 = \cos^2 x$$

$$22. 4 \cos^2 x - 1 = 0$$

For 22-25, Find the exact value of each trigonometric expression.

$$23. \cos \frac{5\pi}{12}$$

$$24. \sin (195^\circ)$$

$$25. \tan 345^\circ$$

$$26. \tan \left(\frac{23\pi}{12} \right)$$